

**Příklady k přednášce 11**  
**Exercises for Lecture 11**

1. Consider two systems,  $S_1 = (A_1, B_1, C_1, D_1)$  and  $S_2 = (A_2, B_2, C_2, D_2)$ , given by  $A_1 = -1, B_1 = 1, C_1 = -2, D_1 = 1$  and  $A_2 = -1, B_2 = 2, C_2 = 1, D_2 = 0$  that are connected in parallel. Determine a state description,  $(A, B, C, D)$ , of the overall system. Is the overall system controllable? Is it observable? Calculate the transfer function of the overall system.

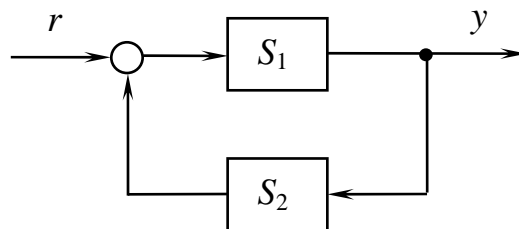
2. Consider two systems,  $S_1 = (A_1, B_1, C_1, D_1)$  and  $S_2 = (A_2, B_2, C_2, D_2)$ , given by  $A_1 = 0, B_1 = 1, C_1 = 1, D_1 = 0$  and  $A_2 = -1, B_2 = -1, C_2 = 1, D_2 = 1$ .

(a) Connect the two systems in series so that  $S_1$  precedes  $S_2$  and determine a state representation,  $(A, B, C, D)$ , of the overall system. Is the overall system controllable? Is it observable?

(b) Connect the two systems in series so that  $S_1$  follows  $S_2$  and determine a state representation,  $(\bar{A}, \bar{B}, \bar{C}, \bar{D})$ , of the overall system. Is the overall system controllable? Is it observable?

Calculate the transfer functions of the overall systems under (a) and (b).

3. Consider the feedback interconnection of two systems,  $S_1$  and  $S_2$ , shown below



Given the state representations of  $S_1$  and  $S_2$  by

$$A_1 = -1, B_1 = 1, C_1 = -1, D_1 = 1 \quad \text{and} \quad A_2 = 0, B_2 = 1, C_2 = 1, D_2 = 0,$$

- (a) determine a state representation of the feedback configuration,  $S$ ,
- (b) determine stability, controllability and observability properties of  $S$ ,
- (c) obtain the transfer function of  $S$  between  $y$  and  $r$ .

4. Consider the double integrator

$$H_1(s) = \frac{1}{s^2}.$$

Characterize the set of all stabilizing controllers  $H_2$  for  $H_1$ , with  $H_2$  proper rational. Does this set contain a stabilizing controller of McMillan degree zero?

5. Consider

$$H_1(s) = \begin{bmatrix} \frac{1}{s^2} \\ \frac{1}{s} \end{bmatrix}.$$

Derive doubly coprime proper and stable matrix fraction representations of  $H_1$  and characterize all proper stabilizing controllers  $H_2$  for  $H_1$ .